

# Cryptocurrencies and (PoW) Distributed Consensus

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## Science of Nakamoto Consensus

[Garay-Kiayias-Leonardos'15] [Kiayias-Panagiotakos'15] [Pass-Seeman-Shelat17]

- **chain growth:** chain grows proportionally with the number of time steps
- **chain quality/blockchain quality/fairness:** fraction of blocks proportional to mining power
- **(blockchain) consistency:** agreement among players on blockchain except for last  $\sigma$  blocks
- **liveliness:** no transaction censorship

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## Science of Nakamoto Consensus

[PSS17] Rafael Pass, Lior Seeman, and Abhi Shelat. Analysis of the blockchain protocol in asynchronous networks. Eurocrypt'17

**Theorem 2.6** (Security of Nakamoto [PSS17]). *For any constant  $\delta > 0$ , any  $0 < p < 1$ , any super-logarithmic function  $T_0 = \omega(\log \kappa)$  Nakamoto's blockchain protocol  $\Pi_{\text{nak}}(p)$  satisfies the following properties in  $\Gamma_{\text{nak}}^p$ -environments:*

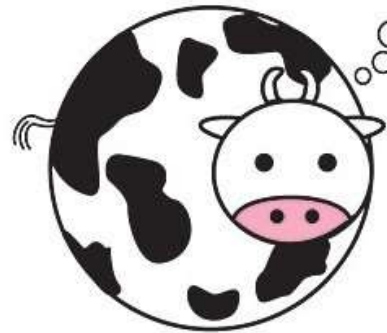
- $T_0$ -consistency;
- chain growth rate  $(T_0, g_0, g_1)$  where

$$g_0 = (1 - \delta)\gamma$$

$$g_1 = (1 + \delta)np$$

- chain quality  $(T_0, \mu)$  where

$$\mu = 1 - (1 + \delta)\frac{\beta}{\gamma}$$



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Tortoise and  
Publish or  
Perish  
Hares  
RAHACK'S IDEA  
SUBCHAINS  
BYZCOIN  
GOSHAWK  
BITCOIN-NG (AETERNITY, WAVES)  
BITCOIN'S NAKAMOTO CONSENSUS  
DECOR+ (ROOTSTOCK)  
ETHEREUM POW  
GHOST-DAG  
SPECTRE  
CHAINWEB  
FRUITCHAINS  
PHANTOM  
GHOST  
BOBTAIL  
THE INCLUSIVE PROTOCOL  
Conflux

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## Bitcoin's Nakamoto Consensus

NC



- To resolve fork
  - Longest chain (roughly) if there is one
  - First-received in a tie
- To issue rewards
  - Main chain blocks ▲ receive full rewards
  - Orphaned blocks △ receive nothing

Key Weakness

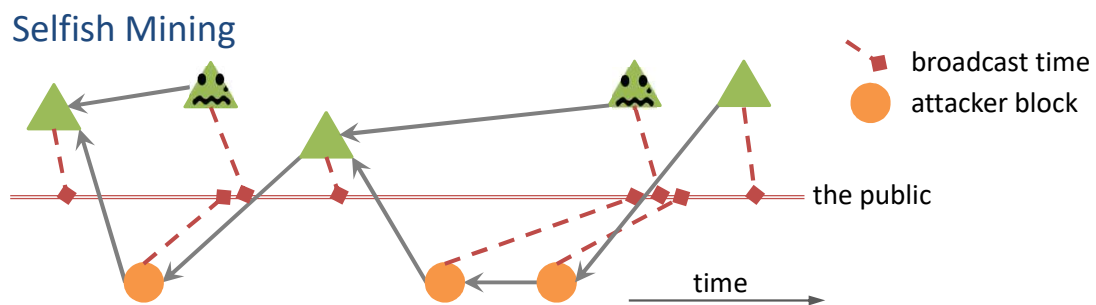
- imperfect chain quality:  
a <50% attacker can modify the blockchain  
with high success rate

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## Imperfect Chain Quality ☞ 3 Attacks

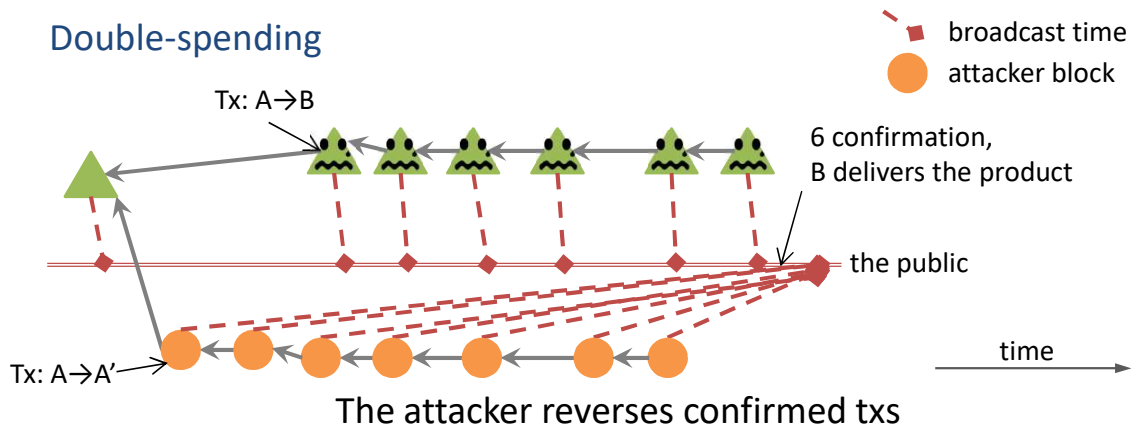


The attacker gains unfair block rewards; rational miners would join the attacker, which damages decentralization

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## Imperfect Chain Quality ☞ 3 Attacks

### Double-spending

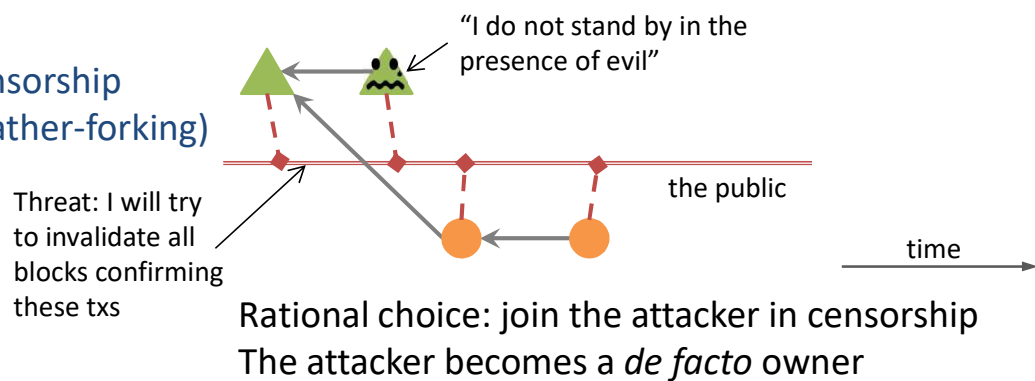


Subversion bounty = minimum double-spending reward to incentivize attack attempts

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## Imperfect Chain Quality ☞ 3 Attacks

### Censorship (feather-forking)



These 3 attacks are **most influential**.

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## Other attacks

– out of scope as beyond pure consensus protocol

- [Bonneau'16] ■ Renting mining equipment
- Bribing miners
- [Meshkov+'17] ■ Coin hopping (based on difficulty adjustments)
- [Eyal'15] ■ Attacks on mining pools
- [Kwon+'17]
- [Carlsten+'16] ■ If block rewards shrink: claim less transaction
- [Tsabary+'18] fees on fork so miners join for remaining higher fees

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## Our Evaluation Framework: Four Metrics

- A protocol claims to be more secure than NC:
- it either ■ achieves better chain quality
  - or ■ resists better against all three attacks:
    - selfish mining ↪ incentive compatibility (revenue)
    - double-spending ↪ subversion gain
    - censorship ↪ censorship susceptibility

Byzantine adversaries rather than rational  
(check [Zhang-P'19] for the math definitions)

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## Candidates



### Better-chain- quality protocols

[tie breaking rule]

#### ■ “I can raise the chain quality”

- **UTB**: Ethereum PoW, Bitcoin-NG (Aeternity, Waves)
- **SHTB**: DECOR+ (Rootstock)
- **UDTB**: Byzcoin, Omniledger
- Publish or Perish

### Attack-resistant protocols

[topology/reward  
distribution]

this talk

check [Zhang-P’19]

#### ■ “I don’t need to raise the chain quality, I can defend against the attacks”

- **Reward-all** (“compensate the losers”): **FruitChains**,  
Ethereum PoW, Inclusive, SPECTRE, PHANTOM, ...
- **Punishment** (“fine all suspects”): **DECOR+**, Bahack’s idea
- **Reward-lucky** (content-based reward): **Subchains**, Bobtail

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## Attack model

- Attacker works on a single chain
- Ignore transaction fees
- Expected block interval identical for all protocols
- Zero natural orphan rate (low delay)

Longest chain rule + rational attacker: can prove  
that there are at most two chains: public/attacker

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## MDP-based Method

[Saphirstein-Sompolinsky-Zohar, FC'16]

1. Define **the attacker's utility** according to the security metric of interest
2. Model the consensus protocol as a **Markov decision process (MDP)**
3. Compute the attacker's **optimal strategies** and their maximum utilities in various settings

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## MDP description

S: State space

A: Action space

P: Stochastic transition matrix

R: Reward matrix

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## MDP: Action space A for Bitcoin

**a** length of attacker's chain after last fork

**h** blocks of honest miner's chain after last fork

**Adopt:** attack accepts honest network chain; discard **a** attacker blocks

**Override:** attacker publishes his blocks to form longest chain (**a** > **h**)

**Match:** most recent block was published by honest miners; attacker publishes a block to create a tie

**Wait:** attacker keeps mining

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## MDP: State space for Bitcoin

(**a**, **h**, fork)

**a** length of attacker's chain after last fork

**h** blocks of honest miner's chain after last fork

fork:

**relevant:** previous state was of form (**a**, **h-1**, \*)

(**a** ≥ **h**, match is feasible)

**irrelevant:** previous state was of form (**a-1**, **h**, \*)

match not feasible

**active:** honest network is already split due to a match

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## MDP: Transition and reward matrices

Prob.  $\alpha$  Initial state is  $(1,0,\text{irrelevant})$

Prob.  $1-\alpha$  Initial state is  $(0,1,\text{irrelevant})$

Reward: (accepted attacker blocks, accepted honest blocks)

| State $\times$ Action                                                                    | State                             | Probability                       | Reward       |
|------------------------------------------------------------------------------------------|-----------------------------------|-----------------------------------|--------------|
| $(a, h, \cdot), \text{adopt}$                                                            | $(1, 0, \text{irrelevant})$       | $\alpha$                          | $(0, h)$     |
|                                                                                          | $(0, 1, \text{irrelevant})$       | $1 - \alpha$                      |              |
| $(a, h, \cdot), \text{override}^\dagger$                                                 | $(a - h, 0, \text{irrelevant})$   | $\alpha$                          | $(h + 1, 0)$ |
|                                                                                          | $(a - h - 1, 1, \text{relevant})$ | $1 - \alpha$                      |              |
| $(a, h, \text{irrelevant}), \text{wait}$<br>$(a, h, \text{relevant}), \text{wait}$       | $(a + 1, h, \text{irrelevant})$   | $\alpha$                          | $(0, 0)$     |
|                                                                                          | $(a, h + 1, \text{relevant})$     | $1 - \alpha$                      | $(0, 0)$     |
| $(a, h, \text{active}), \text{wait}$<br>$(a, h, \text{relevant}), \text{match}^\ddagger$ | $(a + 1, h, \text{active})$       | $\alpha$                          | $(0, 0)$     |
|                                                                                          | $(a - h, 1, \text{relevant})$     | $\gamma \cdot (1 - \alpha)$       | $(h, 0)$     |
|                                                                                          | $(a, h + 1, \text{relevant})$     | $(1 - \gamma) \cdot (1 - \alpha)$ | $(0, 0)$     |

$^\dagger$  feasible only when  $a \geq h$   
 $^\ddagger$  feasible only when  $a \geq h$

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## MDP challenges

Objective function is non-linear

Can only solve for finite state space (size  $10^7$ ):

simplified attack strategies: bounds

estimate truncation error

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## MDP-based Method

1. Define the attacker's utility according to the security metric of interest
2. Model the consensus protocol as a Markov decision process (MDP)
3. Compute the attacker's optimal strategies and their maximum utilities in various settings
4. Compare the utilities with NC, find out **when they are better/worse**
5. Check the respective strategies, find out **why**

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## Cows Are Not Round in Reality



Do not equate the security of a consensus protocol with its cryptocurrency

- Many **real-world factors** affect the attack difficulty (e.g., 51% attack against ETC vs. against Bitcoin)
- Several systems introduce **extra protection** after we started this work

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## Simplified “Better-Chain-Quality” Results

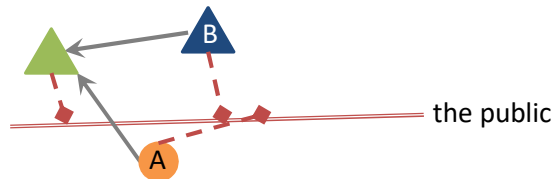
😊 better  
😐 it depends  
😞 worse

| “Better-chain-quality” Protocol                                             | Chain Quality                     |
|-----------------------------------------------------------------------------|-----------------------------------|
| Uniform tie-breaking<br>Ethereum PoW, Bitcoin-NG (Aeternity, Waves)         | 😞 (omitted here, check the paper) |
| Smallest-hash tie-breaking<br>DECOR+ (Rootstock)                            | ?                                 |
| Unpredictable deterministic tie-breaking<br>DÉCOR+LAMI, Byzcoin, Omniledger | ?                                 |
| Publish or perish                                                           | 😐 (omitted here, check the paper) |

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## Better-Chain-Quality: SHTB & UDTB

$\gamma$  = fraction of nodes to which attacker can send blocks first (in case of a tie)



Smallest hash tie-breaking (SHTB)

Unpredictable deterministic tie-breaking (UDTB)

NC,  $\gamma=0.5$

- Compare  $H(A)$  and  $H(B)$ : break the tie with **the smallest hash** regardless of which one is received first
- Compare, e.g.,  $F_k(A \oplus B, A)$  and  $F_k(A \oplus B, B)$ : break the tie with **a deterministic PRF** regardless of which one is received first
- First received tie-breaking; when two chains broadcast simultaneously, choose randomly

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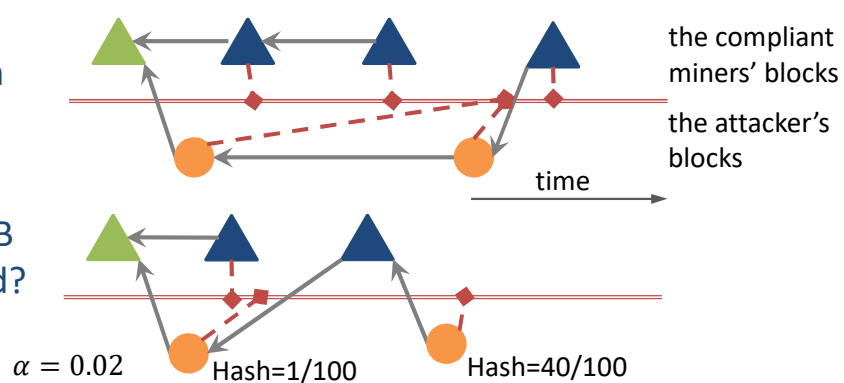
## Chain Quality of Better-Chain-Quality

Ranking

NC,  $\gamma = 0.5 > \text{UDTB} > \text{SHTB}$

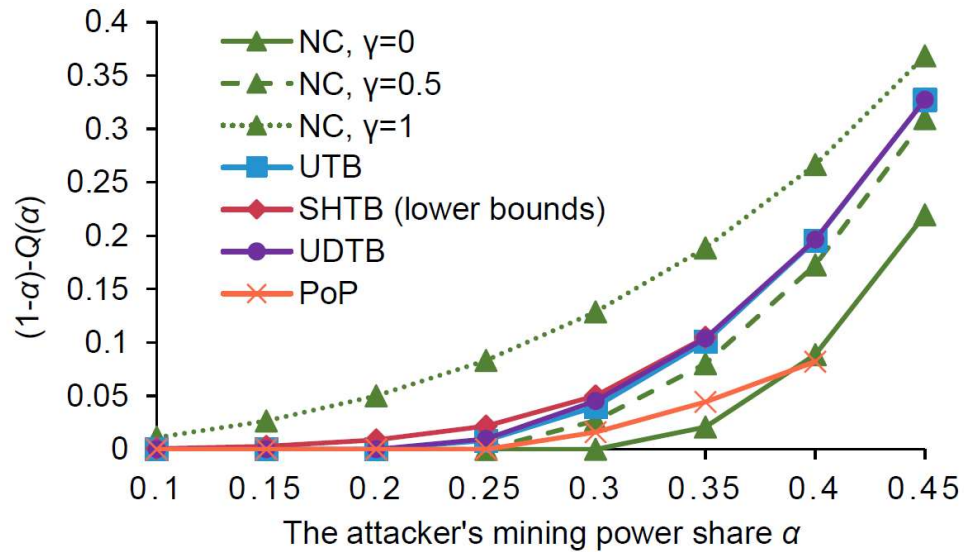
Why is NC,  $\gamma = 0.5$  better than UDTB?

Why does SHTB perform so bad?



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### Simplified “Better-Chain-Quality” Results



### Simplified “Better-Chain-Quality” Results

- 😊 better
- 😐 it depends
- 😞 worse

| “Better-chain-quality” Protocol                                             | Chain Quality |
|-----------------------------------------------------------------------------|---------------|
| Uniform tie-breaking<br>Ethereum PoW, Bitcoin-NG (Aeternity, Waves)         | 😞 worse       |
| Smallest-hash tie-breaking<br>DECOR+ (Rootstock)                            | 😞 worse       |
| Unpredictable deterministic tie-breaking<br>DECOR+LAMI, Byzcoin, Omniledger | 😞 worse       |
| Publish or perish                                                           | 😐 it depends  |

## Better-Chain-Quality Protocols: General Results

- **No protocol** achieves the ideal chain quality when the attacker mining power  $\alpha > 1/4$
- **No protocol** performs better than NC,  $\gamma = 0$  for all  $\alpha$
- Why? ■ The protocols cannot distinguish between honest/attacker blocks
- Why can't they? ■ **Information asymmetry**: the attacker acts on all info; compliant miners do not
- Why don't they? ■ **Inconsistent assumptions**: (try to be) asynchronous, acting on limited public info<sup>29</sup>

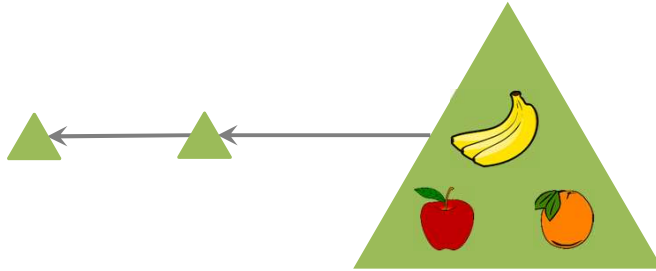
## "Attack-Resistant" Results

😊 better  
😐 it depends  
😞 worse

| "Attack-resistant" Protocol      | Incentive compatibility | Subversion gain | Censorship susceptibility |
|----------------------------------|-------------------------|-----------------|---------------------------|
| Reward-all<br>👉 FruitChains      | ?                       | ?               | ?                         |
| Punishment<br>👉 Reward-splitting | ?                       | ?               | ?                         |
| Reward-lucky<br>👉 Subchains      | ?                       | ?               | ?                         |

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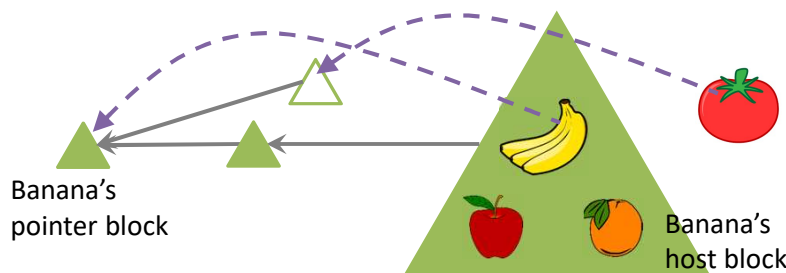
## Attack-Resistant Reward-All: FruitChains



- Same mining procedure, two products:
  - A **block** if the **first** k bits of  $H(\text{candidate}) < D1$
  - A **fruit** if the **last** k bits of  $H(\text{candidate}) < D2$
- Fruits in blocks; txs in fruits
- Fork-resolving: longest chain + first received (same as NC, RS and Subchains)

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## Attack-Resistant Reward-All: FruitChains



Why: stop attackers who generate and hide fruits during a long time and publish them at once

- Each fruit has a **pointer block**: a recent block the fruit miner is sure will not be orphaned
- A fruit is valid if **both conditions are met**:
  - the pointer block is in the main chain (sorry tomato)
  - $\text{Gap}(\text{fruit}) = \text{height}(\text{host}) - \text{height}(\text{pointer}) < \text{TimeOut}$
- Valid fruits receive rewards; blocks, nothing

## FruitChains [Pass-Shi'17]

### Why selfish mining fails

“[...] even if an adversary tries to erase some block mined by an honest player (which contains some honest fruits), by the chain growth and chain quality properties of the underlying blockchain, eventually an honest player will mine a new block which is stable and this honest player will include the fruits” (and fruit will still be “fresh”)

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## FruitChains Results [Pass-Shi'17]

**Theorem 4.1** (Security of FruitChain). *For any constant  $0 < \delta < 1$ , and any  $p, p_f$ , let  $R = 17$ ,  $\kappa_f = 2qR\kappa$ , and  $T_0 = 5\frac{\kappa_f}{\delta}$ . Then the FruitChain protocol denoted  $\Pi_{\text{fruit}}(p, p_f, R)$  satisfies*

- $\kappa_f$ -consistency;
- chain growth rate  $(T_0, g_0, g_1)$  where

$$g_0 = (1 - \delta)(1 - \rho)np_f,$$

$$g_1 = (1 + \delta)np_f$$

- fairness  $(T_0, \delta)$ .

in  $\Gamma_{\text{fruit}}^{p, p_f, R}$ -environments.

No parameters specified

Confirmation time increases with  $T_0$

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## FruitChains Results

😊 better  
😐 it depends  
😞 worse

| "Attack-resistant"<br>Protocol | ① Incentive<br>compatibility | ② Subversion<br>gain | ③ Censorship<br>susceptibility |
|--------------------------------|------------------------------|----------------------|--------------------------------|
| Fruitchains                    | 😐                            | 😞                    | 😊                              |

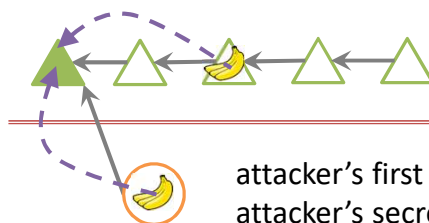
- ①
- Risk-free units -> more audacious behaviors: attacker uses **worthless blocks** to invalidate honest fruits
- ②: less financial risk to attack
- In NC, a failed double-spending attempt results in **losing all block rewards**; in FruitChains, the attacker **gets the first several fruit rewards**

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## FruitChains Results

😊 better  
😐 it depends  
😞 worse

| "Attack-resistant"<br>Protocol | ① Incentive<br>compatibility | ② Subversion<br>gain | ③ Censorship<br>susceptibility |
|--------------------------------|------------------------------|----------------------|--------------------------------|
| Fruitchains                    | 😐                            | 😞                    | 😊                              |



attacker's first fruits: guaranteed rewards  
attacker's secret blocks: no reward anyway  
No risk for double-spending!

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## FruitChains Results

😊 better  
😐 it depends  
😞 worse

| "Attack-resistant"<br>Protocol | ① Incentive<br>compatibility | ② Subversion<br>gain | ③ Censorship<br>susceptibility |
|--------------------------------|------------------------------|----------------------|--------------------------------|
| Fruitchains                    | 😐                            | 😞                    | 😊                              |

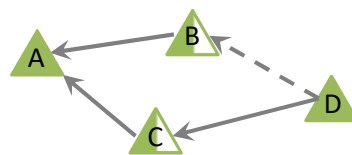
① and ②

Better in ③

- More fruits makes things slightly better
- Fruits in invalidated blocks might be added back later (communication overhead) – unless attacker wins a (long) block race

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## Attack-Resistant Punishment: RS



B's host block: D  
Gap(B)=1

No pointer, unlike Fruitchains

- An **uncle** is valid if
  - $\text{Gap}(\text{uncle}) = \text{height}(\text{host}) - \text{height}(\text{uncle}) < \text{TimeOut}$
- Each block reward is **evenly split** among competing block & uncles of the same height
 
$$R(B) = R(C) = 0.5R(A) = 0.5R(D)$$

(Note: RS is modified from DECOR+, but their results are not the same!)

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## RS Results

😊 better  
 😐 it depends  
 😞 worse

| "Attack-resistant" Protocol | ① Incentive compatibility | ② Subversion gain | ③ Censorship susceptibility |
|-----------------------------|---------------------------|-------------------|-----------------------------|
| Reward-splitting            | 😊                         | 😊                 | 😐                           |

Better than NC in ① and ②

- 3-confirmation RS performs better than 9-conf. FruitChains (risk of withholding a block)

Subversion Bounty

- If  $\alpha = 0.1$ , 6 block confirm., subversion bounty = 0 block rewards in Fruitchains, 102 in NC, 346 in RS

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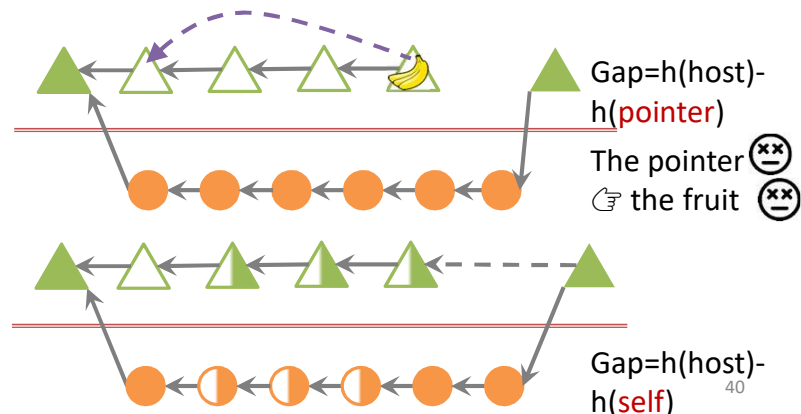
## Censorship Susceptibility of RS

Rankings

For small  $\alpha$ : Fruitchains < NC < RS (not good)

For big  $\alpha$ : RS (best), Fruitchains < NC

Why can RS defend against strong attackers?



## Attack-Resistant Reward-Lucky: Subchains



- Same mining procedure, two products:
  - A **block** if  $H(\text{candidate}) < D1$
  - A **weak block** if  $D1 < H(\text{candidate}) < D2$
- Weak blocks count in chain length, confirm txs
- Only blocks receive block rewards

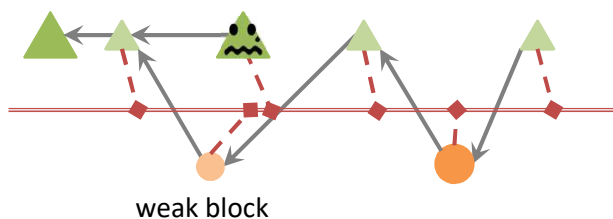
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## Subchains Results

 better  
 it depends  
 worse

| "Attack-resistant" Protocol | ① Incentive compatibility                                                           | ② Subversion gain                                                                   | ③ Censorship susceptibility                                                           |
|-----------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------|
| Subchains                   |  |  |  |

Worst in ①, ② and ③



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## Subchains Results

😊 better  
 😐 it depends  
 😞 worse

| "Attack-resistant" Protocol | ① Incentive compatibility | ② Subversion gain | ③ Censorship susceptibility |
|-----------------------------|---------------------------|-------------------|-----------------------------|
| Subchains                   | 😞                         | 😞                 | 😞                           |

Worst in ①, ② and ③

- Risk-free units -> more audacious behaviors: Subchains allow attacker to use **worthless weak blocks** to invalidate honest blocks
- More weak blocks makes things worse

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## Simplified Results

😊 better  
 😐 it depends  
 😞 worse

| "Better-chain-quality"                   | Chain Quality | "Attack-resistant"              | Incentive compatibility | Subversion gain | Censorship susceptibility |
|------------------------------------------|---------------|---------------------------------|-------------------------|-----------------|---------------------------|
| Uniform tie-breaking                     | 😞             |                                 |                         |                 |                           |
| Smallest-hash tie-breaking               | 😞             |                                 |                         |                 |                           |
| Unpredictable deterministic tie-breaking | 😞             |                                 |                         |                 |                           |
| Publish or perish                        | 😐             |                                 |                         |                 |                           |
|                                          |               | Reward-all<br>👉Fruitchains      | 😐                       | 😞               | 😊                         |
|                                          |               | Punishment<br>👉Reward-splitting | 😊                       | 😊               | 😐                         |
|                                          |               | Reward-lucky<br>👉Subchains      | 😞                       | 😞               | 😞                         |

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## Attack-Resistant Protocols: General Results

### Security vs. Performance

- Longer confirmation helps
- More bandwidth consumption may help

### Dilemma

“Rewarding the bad vs. punishing the good”

- Reward all -> no risk to double-spend
- Punish -> aid censorship
- Reward lucky -> lucky ≠ good

Need to go beyond reward distribution policy to solve all attacks

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## Discussion

### NC rocks!

### What not to do

- Simplicity is beauty
- Designing protocols too complicated to analyze
- Security analysis against one attack strategy
- Security analysis against one attacker incentive
- Security analysis with unrealistic or unspecified parameters

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## Discussion

### Better chain quality & attack resistance?

#### Practical assumptions

- Awareness of network conditions
- Loosely synchronized clock
- Real-world commitments

#### Outsource liability to raise attack resistance

- Introduce additional punishment rules (embed proofs of malicious behavior in blockchain)
- Solve at layer 2 (e.g. lightning guarantees double spending resistance)

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## Want to know more?

- J.A. Garay, A. Kiayias, N. Leonardos, The Bitcoin backbone protocol: Analysis and applications, Eurocrypt'15
- R. Pass, L. Seeman, A. Shelat. Analysis of the blockchain protocol in asynchronous networks. Eurocrypt'17
- A. Sapirshtein, Y. Sompolinsky, and A. Zohar, Optimal selfish mining strategies in Bitcoin, Financial Cryptography and Data Security, 2016.
- R. Zhang, B. Preneel, On the Necessity of a Prescribed Block Validity Consensus: Analyzing Bitcoin Unlimited Mining Protocol, ACM CoNEXT '17
- R. Zhang, B. Preneel, Lay Down the Common Metrics: Evaluating Proof-of-Work Consensus Protocols' Security, IEEE Symposium on Security and Privacy (SP 2019)

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Thank you!

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NERVOS COSIC



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